

# Including Soil Drying Time in Cable Ampacity Calculations

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**Abstract**—Previous papers proposed a method to find the maximum possible dried area of soil expected due to heating by underground cables. A method was also proposed to include this dried soil area in cable ampacity calculations. This assumed that cables would be loaded 100% of the time. To dry soil to the maximum possible extent may take very long time periods, and in many installations, the cables actually carry current for a limited time. In these cases, the soil may never dry to its maximum extent. This paper proposes a method to approximately determine the radius of dried soil that will occur due to cable heating for limited periods of time. It similarly proposes a method to approximate the time it will take for the dried soil to be replenished to its original moisture content after heating by the cables has ceased.

**Index Terms**—Power cable thermal factors, power cables, soil, soil thermal stability, thermoresistivity, underground power distribution, underground power transmission.

## DEFINITION OF VARIABLES

$\Delta T_{cnew}$	Change in temperature between the heated source and ambient soil temperature at the new heat conduction rate $q_{cnew}$ found using (4) (°C).
$\Delta T_{NHR}$	Change in temperature between the heated source and ambient soil temperature at the nondrying heat rate, $q_{NHR}$ , measured during field testing. $T_1 - T_2$ in (2) (°C).
$\gamma$	Unit weight of soil (g/cm <sup>3</sup> ).
$\gamma_w$	Unit weight of water per volume of soil (g/cm <sup>3</sup> ).
$\rho$	Soil thermal resistivity cm-°C/W.
$\omega$	water content in per unit (%/100).
$C_w$	Specific heat of water (4.18 J/g-°C).
$D$	Maximum dried soil diameter (cm).
$D_2$	Diameter of the dried area of soil (cm).
$D_{probe}$	Diameter of the probe used in measuring the nondrying heat rate (cm).
$h_v$	Heat of vaporization of water (2 260 J/g).
$L$	Length of probe below the earth's surface (cm).
$M$	Mass of water in a volume one cm thick bounded by $r_1$ and $r_2$ (g).

$M_{in}$	Rate of water flow into a dried area one cm thick (g/s).
$M_{inavg}$	Average flow rate of water into a dried area 1-cm thick bounded by $r_1$ and $r_2$ (g/s).
$M_{out}$	Rate of water flow out of the dried area 1-cm thick caused by the heat source (g/s).
$M_{return}$	Rate water will return to the dried area of soil 1-cm thick (g/s).
$q_{new}$	Heat rate of the cable under consideration (W/cm).
$q_{cnew}$	Heat carried away by conduction found using (3) (W/cm).
$q_{NHR}$	Nondrying heat rate from field measurements (W/cm).
$q_{cNHR}$	Heat carried away by conduction at the nondrying heat rate (2) (W/cm).
$r$	Radius from the center of the heat source to the wet/dry soil interface (cm).
$r_1$	Radius of from the center of the heat source to the inner boundary of the dried soil (cm).
$r_2$	Radius from the center of the heat source to the outer boundary of the dried soil area (cm).
$t$	time (s).
$T_1$	Surface temperature of the probe at the non-drying heat rate (NHR) measured during field testing (°C).
$T_2$	Ambient soil temperature (°C).
$Z$	Constant found in (10).

## I. INTRODUCTION

**B**URIED cables heat the surrounding soil, decreasing the soil's moisture content and increasing the soil's thermal resistance. This gradual drying may eventually cause cable overheating. Previous papers have proposed a method for determining the maximum diameter of the dried soil area and described how this dried area may be included in Neher-McGrath cable ampacity calculations [1], [2]. This method was based upon the worst case assumption that the buried cables would provide a constant heat rate 100% of the time.

Many installations have a load factor that causes cable heating far less than this worst case condition. Many photovoltaic installations deliver power only 6–8 h a day, with very little output the remaining 16–18 h. This heating pattern dries the soil for a few hours but allows moisture from surrounding soil to replenish the dry soil over a longer period of time. Using the maximum possible diameter of dried soil is overly conservative, causing cables to be unnecessarily oversized, resulting in increased cost.

Soil will be subject to drying only during the time the cable is carrying current. A method is proposed to calculate the radius of soil that will dry based on the heating duration. This paper

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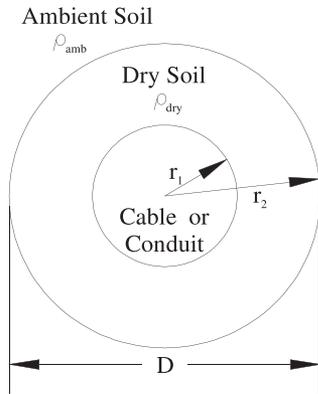


Fig. 1. Model of soil drying.

proposes an approximate method to determine the radius of dry soil that will occur during any arbitrary time period and heat rate. Once this dried soil radius is known, it can be used in cable ampacity calculations in lieu of the maximum possible dried radius. Since the radius of soil around a cable that will dry during a limited time will be less than the maximum possible radius, the result will be an increase in allowable cable ampacity compared to the worst possible case.

## II. SOIL DRYING

Fig. 1 shows the model for soil drying around a cable. The dry soil will have a thermal resistivity of  $\rho_{\text{dry}}$  and the ambient soil thermal resistivity is  $\rho_{\text{amb}}$ . The maximum possible diameter dry soil,  $D$ , that will occur due to the heat produced by a cable, is given by [1]

$$D = D_{\text{probe}} \left( \frac{q_{\text{new}}}{q_{\text{NHR}}} \right). \quad (1)$$

The nondrying heat rate  $q_{\text{NHR}}$  is the highest heat rate at which the soil will not begin to dry using a probe of diameter  $D_{\text{probe}}$ . At any higher heat rate drying will occur. This value is determined by field testing [1]. If the cable is loaded 100% of the time, the soil will eventually dry to the diameter calculated from (1). If the cable is not loaded 100% of the time, the diameter of dried soil may be much less.

A cable loaded for only a few hours a day will dry the soil during those hours. Once heating ceases, the moisture in the surrounding area will replenish the dried area. If the soil can return to its original moisture content before the next heating cycle begins, then the soil will never dry to its maximum possible diameter. If the soil moisture cannot be completely replenished during the time the cable is not heating, then the dried area will continue to expand until it reaches the maximum possible diameter  $D$  calculated in (1). If the dried moisture can be completely replenished during the time the cable is not heating, the maximum extent of dried soil will only reach the diameter that will dry during the time the cable is heating.

When a cable produces heat, the heat is carried away to ambient earth in two main ways. The first is direct conduction through the soil. The second is by vaporizing water. This vapor

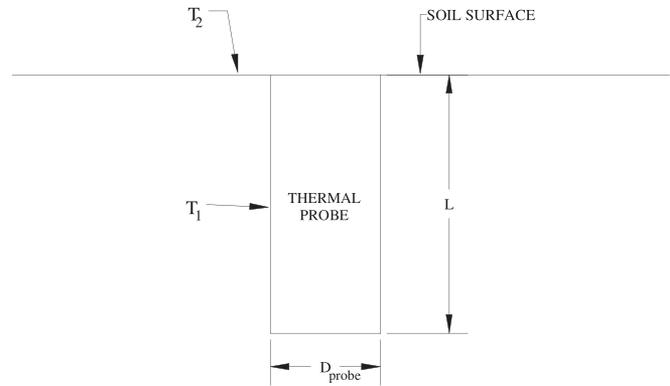


Fig. 2. Thermal probe test for nondrying heat rate.

leaves the vicinity of the cable carrying heat with it. There is also a small amount of heat absorbed by water flowing in to replace the vapor that is heated from ambient temperature to the temperature of the cable surface.

Using the results of field testing for soil resistivity and nondrying heat rate, the value of heat being lost due to conduction under steady-state conditions may be found. A heated cylinder is inserted into the ground as shown in Fig. 2 and the heat rate into the cylinder is set to the nondrying heat rate. The two temperatures  $T_1$ , the temperature of the surface of the heated probe, and the ambient soil temperature are measured. Assuming that  $T_2$  is equal to the average soil ambient temperature and the earth is equivalent to a semiinfinite medium of constant resistivity, the heat conduction through the soil can be found using [1], [3], and [7]

$$q_{\text{cNHR}} = \frac{2\pi (T_1 - T_2)}{\rho \ln \left( \frac{4L}{D_{\text{probe}}} \right)}. \quad (2)$$

The heat rate produced by the cables  $q_{\text{new}}$  may be greater than the nondrying heat rate  $q_{\text{NHR}}$ . Assuming that the heat conducted through the earth,  $q_{\text{cnew}}$ , at a new heat rate,  $q_{\text{new}}$ , will be proportional to the conduction  $q_{\text{new}}$  divided by  $q_{\text{NHR}}$ , the conduction at the new heat rate may be found using

$$q_{\text{cnew}} = \frac{q_{\text{new}}}{q_{\text{NHR}}} q_{\text{cNHR}}. \quad (3)$$

As the radius of dried soil increases, there will be some radius at which the heat rate of conduction to ambient earth will remain constant. This radius is termed the wet/dry soil interface and represents a dry soil annulus from the cable jacket to this radius and ambient soil beyond that point. It occurs for a given cable heat rate  $q_{\text{cnew}}$ . This implies that the temperature at the wet/dry soil interface will also stay constant at the temperature  $T_1$ . It is this radius that is calculated and considered to be the boundary of dried soil. Equation (2) implies that as the diameter of the cylinder of dried soil increases, either the heat rate of conduction will slightly increase, or the wet/dry soil interface temperature  $T_2$  will slightly decrease. For a constant heat rate from the source this would mean the rate of heat carried away by soil moisture would decrease. As a result, making the assumption that the heat

of conduction remains constant will overestimate the amount of drying that will occur, resulting in a conservative design.

Former experiments show that as the diameter of the heat source increases, there is a slight increase in the time it takes to dry soil [4]. This implies that the rate of evaporation decreases as the source diameter increases. If the drying cylinder of soil surrounding the heated source is considered as one composite heat source slowly expanding in diameter, then experimentation also suggests that the time it takes to dry the soil would slowly increase as the diameter of dried soil increases. The proposed method, which assumes that the drying rate and heat of conduction will remain constant as the soil dries, should overestimate the time it takes to dry the soil.

When the heat rate of the source is increased to  $q_{new}$ , the heat rate of conduction increases to  $q_{cnew}$ . The following equation may be used to find the difference in temperature between ambient soil temperature and the temperature of the heated source when the rate of heat leaving the heat source by conduction is equal to  $q_{cnew}$ :

$$\Delta T_{cnew} = \frac{q_{cnew} \rho \ln\left(\frac{4L}{D_{probe}}\right)}{2\pi}. \quad (4)$$

### III. CALCULATING MAXIMUM DRIED SOIL RADIUS

The following equation will be used to calculate the maximum diameter of dried soil that will occur during any given length of time at the heat rate of interest:

$$\begin{aligned} & \text{(Rate of water flow out of a volume of soil) (Drying time)} \\ & - \text{(Rate of water flow into a volume of soil) (Drying time)} \\ & = \text{(Water contained in a volume of soil before drying)}. \end{aligned} \quad (5)$$

If this relationship is satisfied, the volume of soil in question will become dry during the drying time. The volume of soil in (5) is the cross-sectional area of an annulus of soil between radii  $r_1$  and  $r_2$  as shown in Fig. 1, 1 cm in length, surrounding a heated cable or other cylindrical heat source.

Soil testing in the field typically measures the unit weight of the soil and the soil moisture content. If these two values are available, the mass of water within a volume of soil can be calculated using [1]

$$\gamma_w = \frac{\gamma \omega}{1 + \omega}. \quad (6)$$

Once  $\gamma_w$  is found, the mass of water contained within a volume of soil bounded by radii  $r_1$  and  $r_2$  as shown in Fig. 1, and 1 cm thick, may be found using

$$M = (\pi r_2^2 - \pi r_1^2) \gamma_w = \pi \gamma_w (r_2^2 - r_1^2). \quad (7)$$

The rate of water flow out of the area of soil surrounding the heated source may be found using [1]

$$M_{out} = \frac{q_{new} - q_{cnew}}{h_v + C_w \Delta T_{cnew}}. \quad (8)$$

This equation applies when a state of equilibrium has occurred where the soil temperature is not increasing. This would be the

condition when the soil has dried to its maximum extent and the water flow into the dried area of the soil equals the vapor flow out of the dried area. For the transitional condition where the soil is drying and continuing to increase in temperature, use of this equation ignores the heat absorbed by the soil particles. This will result in overestimating the amount of soil that will dry. For most cases, the error resulting will be small compared in the time periods considered in most loading cycles. For simplicity, the heat absorbed by the soil particles is ignored in the suggested procedure, resulting in a conservative estimate for the area of dried soil.

The rate of water flow from the surrounding soil back in to the dried soil layer at the wet/dry interface may be found using [1]

$$\begin{aligned} M_{in} &= \frac{q_{NHR} - q_{cNHR}}{D_{probe} (h_v + C_w \Delta T_{NHR})} D_2 \\ &= \frac{2(q_{NHR} - q_{cNHR})}{D_{probe} (h_v + C_w \Delta T_{NHR})} r. \end{aligned} \quad (9)$$

For simplicity, part of (9) is set equal to a constant,  $Z$ .

$$Z = \frac{2(q_{NHR} - q_{cNHR})}{D_{probe} (h_v + C_w \Delta T_{NHR})} \quad \text{g/s} \cdot \text{cm}^2. \quad (10)$$

So, (9) becomes

$$M_{in} = Zr. \quad (11)$$

The average flow rate of water flowing into an area bounded by any two radii,  $r_1$  and  $r_2$ , may be found using

$$M_{inavg} = \frac{1}{r_2 - r_1} Z \int_{r_1}^{r_2} r dr = \frac{Z(r_2 + r_1)}{2}. \quad (12)$$

Equation (5) may now be written as follows using the pieces developed in (7), (8), and (12):

$$M_{out} t - \frac{Z(r_2 + r_1)}{2} t = \pi \gamma_w (r_2^2 - r_1^2). \quad (13)$$

Solving this equation for  $r_2$  as a function of time  $t$  results in

$$r_2^2 + \frac{Z t}{2\pi \gamma_w} r_2 - \frac{M_{out} t}{\pi \gamma_w} - r_1^2 + \frac{Z r_1 t}{2\pi \gamma_w} = 0. \quad (14)$$

The aforementioned equation may then be solved for  $r_2$ , for any time,  $t$ , using the positive solution to the quadratic formula

$$\begin{aligned} r_2 &= \frac{-B + \sqrt{B^2 - 4AC}}{2A}, \quad A = 1 \quad B = \frac{Z t}{2\pi \gamma_w} \\ C &= -\frac{M_{out} t}{\pi \gamma_w} - r_1^2 + \frac{Z r_1 t}{2\pi \gamma_w}. \end{aligned} \quad (15)$$

The radius  $r_2$  would then be the radius of soil that would dry during time  $t$ .

### IV. RETURNING SOIL MOISTURE TO ITS ORIGINAL VALUE

If a cable carries load less than 100% of the time, the soil moisture will have time to become replenished during the time the cable is not generating heat. If the soil moisture is brought back to its natural content before the next heating cycle begins, then the dried soil diameter will never reach the maximum

possible extent described by (1) and will be limited to the radius calculated in (14). This value could then be used for cable ampacity calculations.

Once an area of soil has dried, the average flow rate of water from the surrounding soil that will flow back into the dry area bounded by radii  $r_1$  and  $r_2$  may be found using

$$M_{\text{return}} = \frac{Z(r_2 + r_1)}{2}. \quad (16)$$

The mass of water necessary to replenish the dried area to its original moisture content can be found using (7). The time in seconds  $t_{\text{return}}$  necessary to return the moisture content of the dried area of soil back to its natural value may be found using

$$\begin{aligned} \pi\gamma_w(r_2^2 - r_1^2) &= \frac{Z(r_2 + r_1)}{2}t_{\text{return}} \\ t_{\text{return}} &= \frac{2\pi\gamma_w(r_2 - r_1)}{Z}. \end{aligned} \quad (17)$$

## V. EXAMPLE

To demonstrate how this method might be applied, consider the case where the following criteria have been measured in the field or determined by design restrictions.

- 1) Cable loading cycle = 0.8 W/cm for 6 h, then 0.0 W/cm for 18 h.
- 2) Direct buried cable diameter = 1 in (2.54 cm).
- 3) Soil density  $\gamma = 100 \text{ lbs/ft}^3 = 1.602 \text{ g/cm}^3$ .
- 4) Soil moisture content  $\omega = 14\% = 0.14 \text{ pu}$ .
- 5) Nondrying heat rate  $q_{\text{NHR}} = 0.15 \text{ W/cm}$ .
- 6) Surface temperature of probe at NHR  $T_1 = 34 \text{ }^\circ\text{C}$ .
- 7) Probe diameter  $D_{\text{probe}} = 1.59 \text{ cm}$ .
- 8) Length of probe  $L = 120 \text{ cm}$ .
- 9) Ambient soil temperature  $T_2 = 29 \text{ }^\circ\text{C}$ .
- 10) Soil thermal resistivity  $\rho = 100 \text{ cm}\cdot^\circ\text{C/W}$ .
- 11) Dry soil thermal resistivity  $\rho_{\text{dry}} = 300 \text{ cm}\cdot^\circ\text{C/W}$ .
- 12) Specific heat of soil particles  $C_s = 0.8 \text{ J/g}\cdot^\circ\text{C}$ .

Equation (1) is used to find the maximum possible diameter of dried soil at the new heat rate of 0.8 W/cm

$$D = 1.59 \left( \frac{0.8}{0.15} \right) = 8.48 \text{ cm}.$$

If the load factor of the cable was 100%, then the soil would be expected to dry to a diameter of 8.48 cm. However, since the load cycle of the cable is only 6 h, the diameter of dry soil during those 6 h will be less than this maximum amount.

Using (2), the heat of conduction at the nondrying heat rate is found

$$q_{\text{cNHR}} = \frac{2\pi(34 - 29)}{100 \ln\left(\frac{4(120)}{1.59}\right)} = 0.055 \text{ W/cm}.$$

The expected heat of conduction at the new heat rate is found using (3)

$$q_{\text{cnew}} = \frac{0.8}{0.15} 0.055 = 0.2934 \text{ W/cm}.$$

The difference in temperature between the heat source and the ambient soil at the new heat rate is found using (4)

$$\Delta T_{\text{cnew}} = \frac{0.2934(100) \ln\left(\frac{4(120)}{1.59}\right)}{2\pi} = 26.67 \text{ }^\circ\text{C}.$$

The unit weight of water per volume of soil is found using (6)

$$\gamma_w = \frac{(1.602)0.14}{1 + 0.14} = 0.1967 \text{ g/cm}^3.$$

The rate of water flow out of the dried area is found using (8)

$$M_{\text{out}} = \frac{0.8 - 0.2934}{2260 + (4.18)(26.67)} = 0.0002136 \text{ g/s}.$$

The constant,  $Z$ , is then found using (10)

$$Z = \frac{2(0.15 - 0.055)}{1.59(2260 + 4.18(34 - 29))} = 0.0000524 \text{ g/s}\cdot\text{cm}^2.$$

All the values needed to solve (14) are now available

$$A = 1$$

$$B = \frac{0.0000524 \text{ t}}{2\pi(0.1967)} = 0.0000424 \text{ t}$$

$$\begin{aligned} C &= -\frac{0.0002136}{\pi(0.1967)} \text{ t} - \left(\frac{2.54}{2}\right)^2 + \frac{(0.0000524)\left(\frac{2.54}{2}\right) \text{ t}}{2\pi(0.1967)} \\ &= -0.000346 \text{ t} - 1.613 + 0.0000538 \text{ t}. \end{aligned}$$

The time the cable will heat the soil is 6 h, or 21 600 s. Substituting this value for  $t$  results in the following equation. The solution to this equation will be the radius,  $r_2$ , of soil that will dry in 6 h

$$A = 1$$

$$B = 0.0000424(21\,600) = 0.915$$

$$\begin{aligned} C &= -0.000346(21\,600) - 1.613 + 0.0000538(21\,600) \\ &= -7.92 r_2^2 + 0.915 r_2 - 7.92 = 0, \quad r_2 = 2.39 \text{ cm}. \end{aligned}$$

The results are shown in Fig. 3. In a 6-h drying period at a heat rate of 0.8 W/cm, it would be expected that a radius of 2.39 cm of soil would have dried. The result is that the 2.54 cm cable is surrounded by a layer of dried soil with a diameter of 4.78 cm. This area is then surrounded by natural soil of natural moisture content.

It is also important to know if the dried area will be replenished back to its natural moisture content in the 18 h during which the cable will not be producing heat. Equation (17) is used to find the time it will take to replenish the moisture

$$t_{\text{return}} = \frac{2\pi(0.1967)\left(2.39 - \frac{2.54}{2}\right)}{0.0000524} = 26\,416 \text{ s} = 7.34 \text{ h}.$$

Since the moisture in the dried area can be replenished in less than 18 h, the maximum extent of soil drying should be a

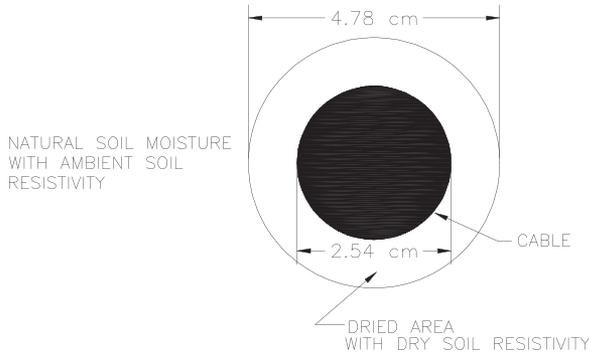


Fig. 3. Cable surrounded with dried soil.

dried soil diameter of 4.78 cm rather than the maximum possible extent of 8.48 cm as calculated using (1). The 4.78 cm will then be used in cable ampacity calculations for this cable. Using this smaller diameter of dried soil will result in a larger cable ampacity and will prevent overdesigning the cable size, thus avoiding unnecessary cost.

## VII. ASSUMPTIONS AND ERRORS

To derive a method of calculating the time and extent of dried soil, that is simple enough to be used in everyday engineering problems, it is necessary to make simplifying assumptions. Each assumption may be a source of error, and the exact impact of these errors is difficult to assess.

Before heating begins, the heat source is surrounded by soil at ambient resistivity and ambient soil moisture. When the heat source is energized, it will take a period of time for its surface temperature to increase to the point that the difference in temperature between the surface of the heat source and ambient soil temperature is  $\Delta T_{cnew}$ . The time needed will depend upon the thermal time constant of the heat source, and this time period is ignored in this procedure.

It is assumed that all moisture movement out of the dried area is due to vapor movement. Some sources claim that some moisture movement out of the dried area occurs due to liquid water movement [5]. Some liquid water movement may occur during the time when the soil is still relatively wet; however, it is reported that as the soil dries, vapor movement becomes the most important component. The proposed method ignores any movement of heat out of the dried area due to liquid water movement.

The procedure assumes that the amount of heat at the NHR can be calculated during a steady state condition, and the heat lost due to conduction at all other heat rates will be proportional to the heat lost due to conduction at the NHR. The magnitude of the error that will result from this assumption, if any, is unknown and will require further experimentation to determine.

When the surface of the heat source increases to a temperature where its surface is equal to the soil ambient temperature plus  $\Delta T_{cnew}$ , soil drying will begin. At this point, a dry/ambient moisture boundary will progress out from the surface of the heat source and become progressively larger until the maximum

extent is reached during the time of interest. It is assumed that the thermal resistance from the surface of this growing cylinder of dried soil to ambient earth will remain constant. The size of the cylinder of dried soil will be controlled by the rate that moisture can flow into the dried area from the surrounding soil and the rate water will evaporate away from the dried area. As the cylinder grows larger, the amount of moisture that can return to the dried area increases.

The temperature at the dry/wet soil interface of the dried cylinder of soil is assumed to be the ambient temperature plus  $\Delta T_{cnew}$ , and the radius of dried soil will be measured to the point where this temperature occurs. While a sudden transition of moisture content and temperature at the wet/dry interface is assumed, it is likely that there will be a gradual transition of both in the wet soil.

Some error will result from ignoring the heat absorbed by the soil particles as the soil heats up from ambient conditions. This error can be estimated.

In the example, after a 6-h period the radius of dried soil progressed to a distance of 2.39 cm from the center of the source. The temperature at this radius would be 55.67 °C (ambient temperature, 29 °C, plus  $\Delta T_{cnew}$ , 26.67 °C). The soil between this boundary layer and the surface of the heat source would have a resistivity equal to the dry soil thermal resistivity,  $\rho_{dry} = 300 \text{ cm}\cdot\text{°C}/\text{W}$ .

Solving the exponential differential equations for transient heat flow through a semiinfinite medium shows that it would take approximately 12 min for the 0.8 W/cm heat source to raise the temperature of a point 2.39 cm from the center of the heat source—in a semiinfinite medium with resistivity = 300 cm·°C/W—by 26.67 °C [6]. So in the 6-h time period, the temperature of the boundary layer would be controlled by moisture flow rather than by the time needed for heat conduction. A quasi-steady state, from the point of view of heat conduction, has developed. Since the dried layer contains no moisture, all the heat flow through it must be due to conduction. Using the steady-state equations for conduction, the temperature of the surface of a heat source of radius 1.27 cm can be determined assuming the soil temperature at a radius of 2.39 cm is being held constant. Using (18), the temperature of the surface of the heat source was found to be 79.82 °C

$$T_1 = \frac{\rho_{dry} q_{new} (\ln r_2 - \ln r_1)}{2\pi} + T_2$$

$$T_1 = \frac{(300)(0.8)(\ln 2.39 - \ln 1.27)}{2\pi} + 55.67 = 79.82 \text{ °C}. \quad (18)$$

Using (19), the temperature at any point a distance  $r$  from the center of the heat source (assuming  $r > r_1$ ) may be found.

$$T_2 = - \left( \frac{\rho_{dry} q_{new} (\ln r - \ln r_1)}{2\pi} - T_1 \right). \quad (19)$$

Fig. 4 shows a plot of the solution to (19) from the surface of the heat source to a radius of 2.39 cm from the center of the heat source.

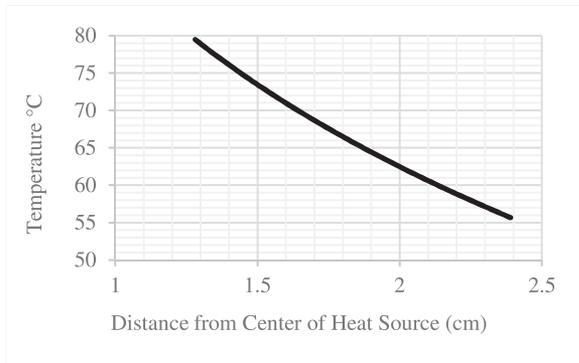


Fig. 4. Temperature from heat source surface to extent of dried area.

Assuming the specific heat of the soil particles is  $0.8 \text{ J/g}\cdot^{\circ}\text{C}$  and a soil particle density of  $1.405 \text{ g/cm}^3$  (total soil  $\text{g/cm}^3$  minus water  $\text{g/cm}^3$ ), a 1-cm depth of soil around the source, heated to the heat gradient shown in Fig. 4, would absorb approximately 523 Joules. At a heat rate of  $0.8 \text{ W/cm}$ , it would take slightly over 10 min to generate 523 J. The 10 min in a 6-h cycle is less than 10%. Furthermore, since 10 min of the heat produced by the heat source during the 6-h heating cycle would be absorbed by the soil particles rather than by the vapor leaving the dried area and the water flowing back into the dried area, the radius of dried soil would be slightly less than the 2.39 cm calculated using this method. The error due to ignoring the heat absorbed by the soil will always be conservative and result in a larger estimation for dried area than should actually occur.

### VIII. CONCLUSION

While using the maximum possible extent of dried soils in Neher–McGrath cable ampacity calculations will result in cables that should not overheat in the presence of soil thermal instability, it is unlikely that the soil will ever dry to this extent in many installations. The soil will dry to the maximum extent only if the time the cable is loaded is greater than the time it takes for moisture from surrounding soil to replenish the dried soil during the time the cable is not loaded. This is a common condition on many projects such as solar and other renewable energy installations with low capacity factors. Also, the same calculations can be used if the cable is loaded less than the nondrying heat rate, i.e., current does not have to be 0 A but can be any value less than the nondrying heat rate to begin rehydrating the soil.

A method is proposed to determine the extent of soil drying when a cable is loaded less than 100% of the time. This method provides an equation to calculate the diameter of dried soil caused by the cable heating above the nondrying heat rate and an equation to calculate the time required to rehydrate this same dried volume. The diameter of dried soil determined using this method may then be used in cable ampacity calculations to account for the effects of thermal instability of the soil due to drying effects. Many commercially available software packages have the ability to include this dried soil diameter by modeling user defined cable insulation or a surrounding duct bank with resistivity equal to the dried soil resistivity. For more details on including these effects, please refer to [2].

The proposed method is currently theoretical. Experimental validation is required and is currently in progress. The experiments must show a change in soil resistivity when the cable heating exceeds the nondrying heat rate and, based on this proposed method, should be time dependent.

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